Hagedorn and Brown

Correlation overview

Mikhail Tuzovskiy 2017



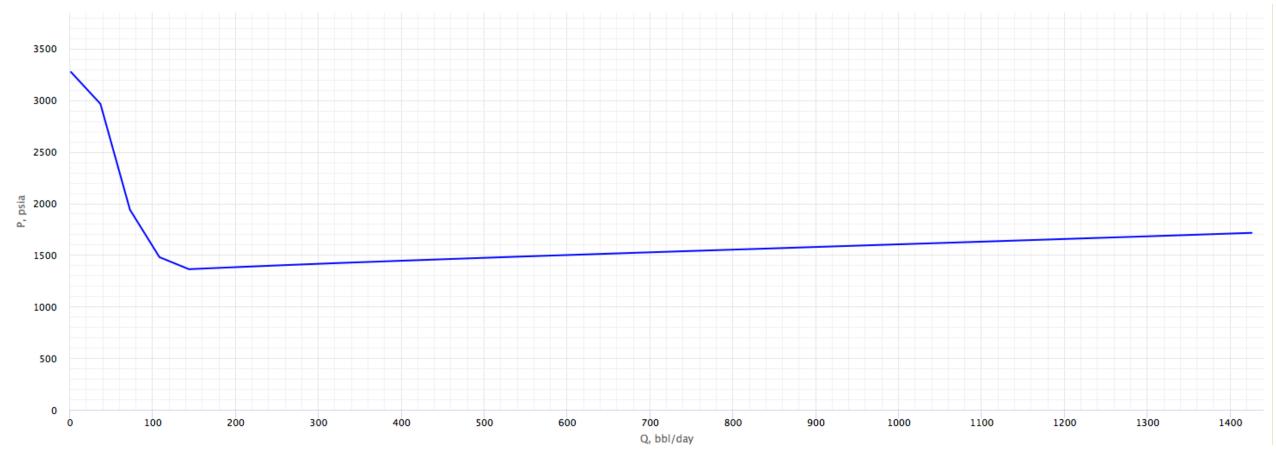
What is the Hagedorn and Brown correlation?

- Multi-phase flow correlation
- Typically used to calculate the VLP curves for the OIL wells
- Hagedorn, A. R.; Brown, K. E. (1965). "Experimental study of pressure gradients
 occurring during continuous two-phase flow in small-diameter vertical conduits". Journal
 of Petroleum Technology. 17(04): 475–484.



What is the VLP curve?

Vertical Lift Performance Curve:

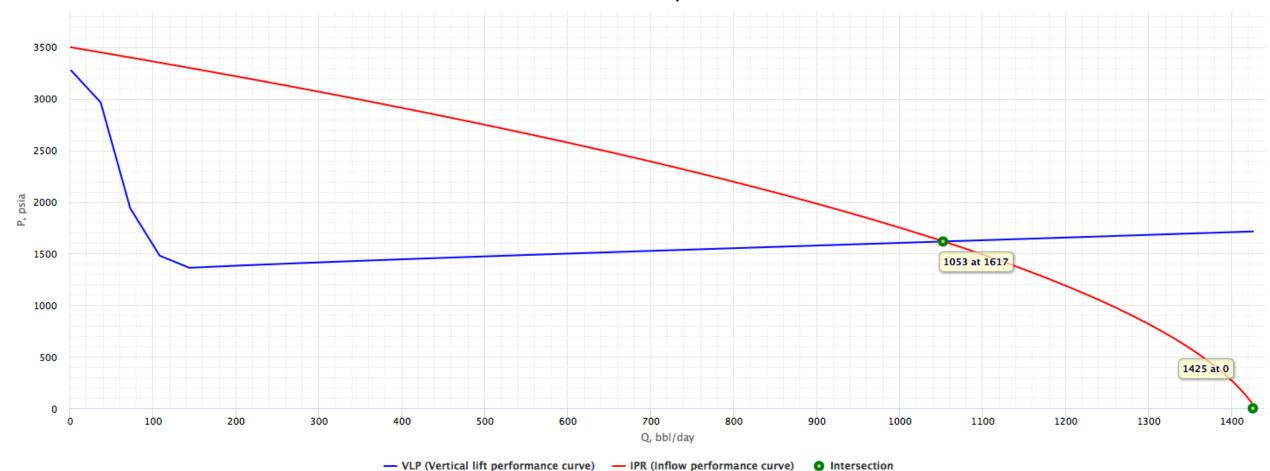


relates how much pressure is required to lift the fluid to the surface



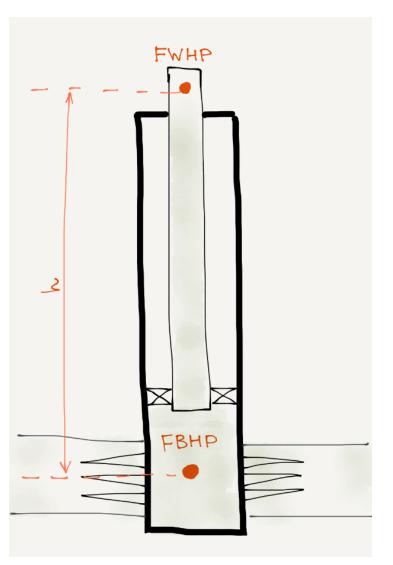
How do we use the VLP curve?

Nodal Analysis:





How to calculate the VLP curve?



$$\frac{dp}{dh} = \left(\frac{dp}{dh}\right)_{GRAVITY} + \left(\frac{dp}{dh}\right)_{FRICTION} + \left(\frac{dp}{dh}\right)_{KINETIC}$$



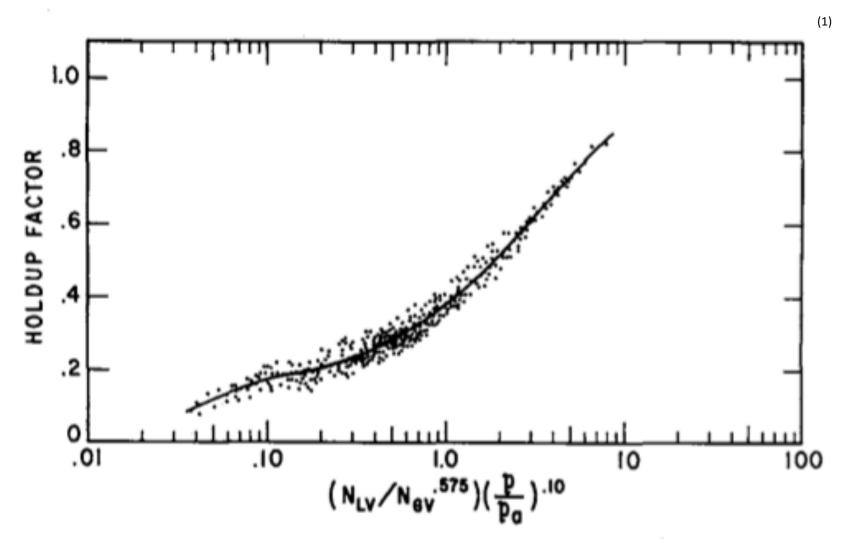
Hagedorn and Brown Math & Physics

$$144 \frac{\Delta p}{\Delta h} = \overline{\rho_m} + \frac{f \ q_L^2 \ M^2}{2.9652 \times 10^{11} \ D^5 \overline{\rho_m}} + \overline{\rho_m} \frac{\Delta \left(\frac{v_m^2}{2g_c}\right)}{\Delta h}$$

$$\overline{\rho_m} = \rho_L H_L + \rho_g (1 - H_L)$$



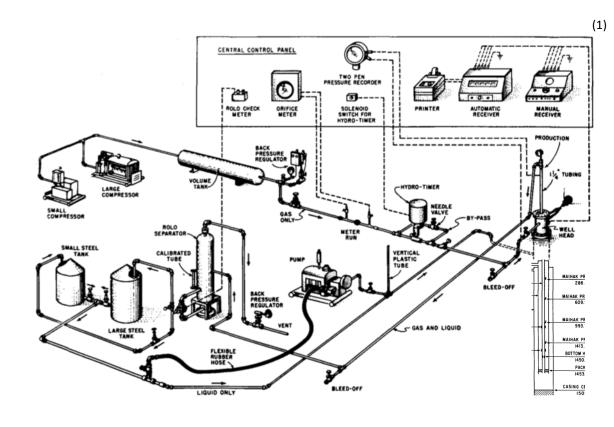
Hagedorn and Brown - H_L





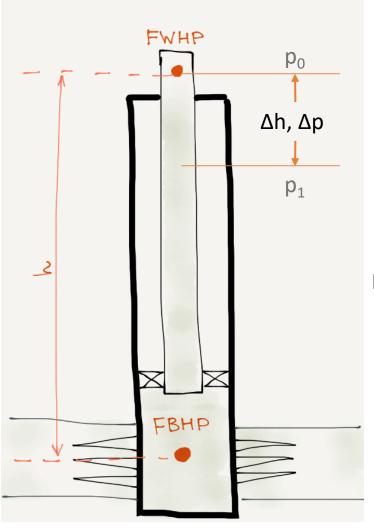
Hagedorn and Brown quick facts

- Test well in Dallas, TX
- Nominal pipe D: 1, 1¼, 1½ in
- Pipe length 1500 ft
- q_L was varied
- For each q_L GOR was varied as well
- Pressure gradient was measured
- 475 tests & 2905 pressure points
- Published in 1965



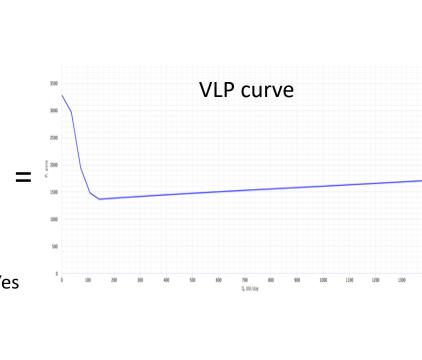


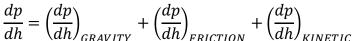
How it works?



Assume Δp_i $p_{i+1}=p_i + \Delta p_i$ Calculate H_L , $\overline{\rho_m}$ For each q_L $Calculate\,\Delta p$ [0 to AOF] $|\Delta p_{i^{\text{-}}} \Delta p|\!\ge\! err$ Yes No Output p_{i+1} at $h+\Delta h$

Select Δh







Finally, how to find H_L?

$$M = SG_o \; 350.52 \; \frac{1}{1 + WOR} + SG_w \; 350.52 \; \frac{WOR}{1 + WOR} + SG_g \; 0.0764 \; GLR^{\text{\tiny [1]}}$$

$$\rho_L = \frac{62.4 \ SG_o + \frac{Rs \ 0.0764 \ SG_g}{5.614}}{B_o} \frac{1}{1 + WOR} + 62.4 \ SG_w \ \frac{WOR}{1 + WOR}^{[5]}$$

$$\rho_g = \frac{28.967 \ SG_g \ p_{\text{[5]}}}{z \ 10.732 \ T_R}$$

$$\mu_L = \mu_o \frac{1}{1 + WOR} + \mu_w \frac{WOR}{1 + WOR}$$
[5]

$$\sigma_L = \sigma_o \frac{1}{1 + WOR} + \sigma_w \frac{WOR}{1 + WOR}$$
[5]

$$N_L = 0.15726 \; \mu_L \sqrt[4]{rac{1}{
ho_L \sigma_L^3}} ^{\text{[1]}}$$

Well, it's a lot of equations:)

$CN_L = 0.061 \ N_L^3 - 0.0929 \ N_L^2 + 0.0505 \ N_L + 0.0019^{[2]}$

$$v_{SL} = \frac{5.615q_L}{86400A_p} \left(B_o \frac{1}{1 + WOR} + B_w \frac{WOR}{1 + WOR} \right)^{[5]}$$

$$v_{SG} = \frac{q_L \left(GLR - R_s \left(\frac{1}{1+WOR}\right)\right)}{86400A_n} \frac{14.7}{p} \frac{T_K}{520} \frac{z_{[5]}}{1}$$

$$N_{LV} = 1.938 \ v_{SL} \ \sqrt[4]{\frac{\rho_L}{\sigma_L}}$$
 [1]

$$N_{GV} = 1.938 \ v_{SG} \ \sqrt[4]{\frac{\rho_L}{\sigma_L}}$$

$$N_D = 120.872 \ D \sqrt{\frac{\rho_L}{\sigma_L}} {}_{\text{[1]}}$$

$$H = \frac{N_{LV}}{N_{GV}^{0.575}} \left(\frac{p}{14.7}\right)^{0.1} \frac{CN_{L_{[2]}}}{N_D}$$

$$\frac{H_L}{\psi} = \sqrt{\frac{0.0047 + 1123.32H + 729489.64H^2}{1 + 1097.1566H + 722153.97H^2}}_{[6]}$$

$$B = \frac{N_{GV} N_{LV}^{0.38}}{N_D^{2.14}}$$
[2]

$$\psi = \begin{cases} 27170B^3 - 317.52B^2 + 0.5472B + 0.9999, & \text{if } B <= 0.025 \\ -533.33B^2 + 58.524B + 0.1171, & \text{if } B > 0.025 \\ 2.5714B + 1.5962, & \text{if } B > 0.055 \end{cases}$$

$$H_L = \frac{H_L}{\psi} \times \psi^{[1]}$$



Summary

- Hagedorn and Brown correlation
- History and practical application
- Math & Physics
- Flow diagram to get the VLP curve
- Workflow to find H₁



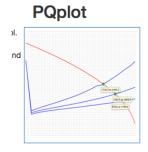
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Thanks!

